Motivation

Examples Bounded Loops

```
for (i = 0; i < max; i++) { do work } while (i > blah) { ... }; do { work } while {i}
```

- Guidelines:
 - Lots of academic work on complex loops
 - polynomial invariants, Grobner basis and more ← fun but lets stick to basic ax+c for now.

Agenda:

```
Review terms, goals, etc.
Approach #1 (by the books)
Approach #2 (compiler aided)
Approach #3 (instruction based)
Discuss
```

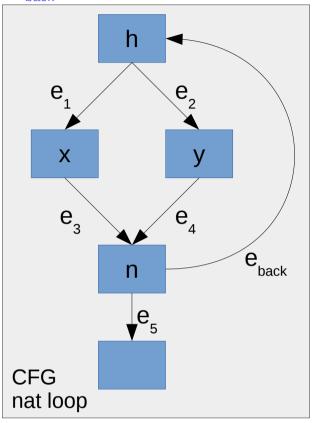
i and j are Induction variables

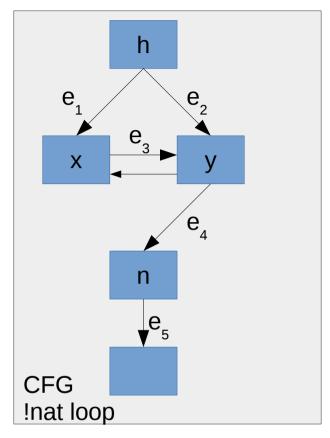
```
int array[10] = init
int max = 10, foo = blah, bar = blah;

for (i = 0; i < max; i++) {
    int j = i * foo + bar;

    value = bpf_map_lookup_elem(&map,
&key);
    if (value > 0)
        sum += array[j]
    else
        sum -= array[j]
}
```

h is a header node e_{back} backedge n->h





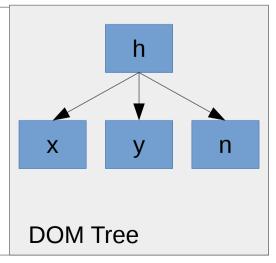
h dominates n, x, y

Natural loop: the set of nodes x, where h dom x with a path from x to n _not_ containing h.

intuition: Does not have multiple goto's into loop.

Find Natural Loop Algorithm:

- 1. Compute CFG and Dominator Tree
- 2. Find back edges
- 3. Find the natural loop using DOM Tree



Approach #1: by the book

https://git.kernel.org/pub/scm/linux/kernel/git/bpf/bpf-next.git/ wip/bpf-loop-detection

- Build CFG
- Build DOM Tree
- Detect and abort on irreducible loops
- Find loops (back edges)
- For Each Loop
 - Find induction variables (pattern matching)
 - Verify bounds on loop induction variable terminate
 - "run" loop with worst case bounds, pruning works, array index worst case.

```
hdr:
<do stuff>
if (i != x) goto hdr
```

hdr:

<do stuff>
if (i != x) goto out
<do more stuff>
goto hdr out:
<outside loop>

Challenge: Many LLVM loop patterns. At the moment we do pattern matching and can extend these but fragile.

PROP1: General forest of Induction variables or SCEV needed.

Approach #2: Compiler Aided

https://git.kernel.org/pub/scm/linux/kernel/git/bpf/bpf-next.git/ wip/bpf-loop-detection

Limit types of loops constructed by LLVM

```
hdr:
<do stuff>
if (i != x) goto hdr
```

- Easy to pattern match if LLVM plays along
- Still need to do full verification of natural loops (build DOM tree, etc.) and find induction variables. But somewhat easier because of friendly LLVM.

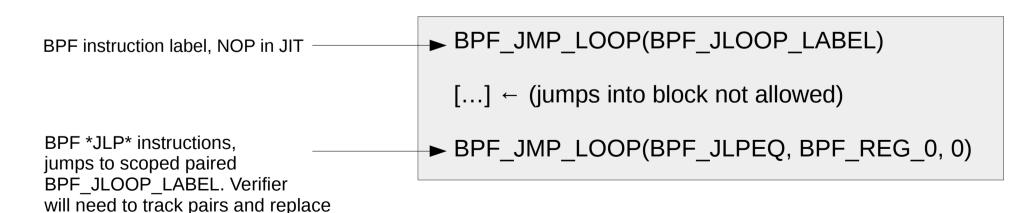
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Approach #3: New instructions

Loop specific instructions

with proper jumps after verification.

- Denote loop blocks with instructions loop/end
- Requires LLVM backend to convert unstructured gotos into structured loops. DOM tree no longer required replaced with strict hierarchy of blocks.
- Ensure goto's into loop blocks fail, overlapping blocks not allowed, induction variable tracking still required.



Discuss

Decide how to proceed and get loop support.